Section 5.2 Frequency and Probability Distributions Math 141

<u>Main ideas</u>

Distribution: possible outcomes.

Frequency distribution: how many times each outcome did occur.

Relative frequency distribution: what *fraction* of the time each outcome **did** occur.

Probability distribution ("expected relative frequency distribution"): what *fraction* of the time each outcome **should** occur.

In histograms, area = probability.

Random variables.

Problems

Probability distribution.
Flip 4 coins. Total number of possible outcomes =

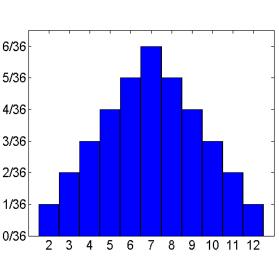
| Outcome | Number | | 6/16 | | | | · · | | |
|-----------|------------|-------------|-------|---|---|---|-----|---|---|
| (number | of ways it | Probability | | | | | | | |
| of heads) | can occur | | 5/16 | | | | | | - |
| 0 | | = | 4/16 | | | | | | - |
| 1 | | = | 3/16- | | | | | | - |
| 2 | | = | 2/16- | | | | | | |
| 3 | | = | | | | | | | |
| 4 | | = | 1/16- | | | | | | - |
| Total | | | 0/16 | 0 | 1 | 2 | 3 | 4 | |

2. Frequency distribution, relative frequency distribution, probability distribution. Flip 4 coins. Record the number of heads for each flip.

| Outcome (number of heads) | Frequency | Relative frequency | Expected relative frequency (probability) |
|------------------------------|-----------|-----------------------|--|
| 0 | | = | .0625 |
| 1 | | = | .2500 |
| 2 | | = | .3750 |
| 3 | | = | .2500 |
| 4 | | = | .0625 |
| Total | | | 1.0000 |

Frequency distribution, relatively frequency distribution, probability distribution.
Roll two dice. Record the sum of each roll.
From a previous semester of this class.

| Sum | # of outcomes | Fraction of Arall outcomes | Expected fraction |
|-------|------------------|----------------------------|-------------------|
| 2 | 15 | 15/926 = .0162 | = .0278 |
| 3 | 73 | 73/926 = .0788 | = .0556 |
| 4 | 69 | 69/926 = .0745 | = .0833 |
| 5 | 94 | 94/926 = .1015 | = .1111 |
| 6 | 130 | 130/926 = .1404 | = .1389 |
| 7 | 150 | 150/926 = .1620 | = .1667 |
| 8 | 125 | 125/926 = .1350 | = .1389 |
| 9 | 110 | 110/926 = .1188 | = .1111 |
| 10 | 80 | 80/926 = .0864 | = .0833 |
| 11 | 55 | 55/926 = .0594 | = .0556 |
| 12 | 25 | 25/926 = .0270 | = .0278 |
| Total | 926 | 1.0000 | 1.0000 |



4. Random variable X is the thing we are interested in for an experiment.

Experiment: flip four coins. Let X = the number of heads.

| k | Pr(X = k) |
|---|-----------|
| 0 | |
| 1 | |
| 2 | |
| 3 | |
| 4 | |

Experiment: roll two dice. Let X = the sum of dice.

| k | Pr(X = k) |
|---|-----------|
| | |
| | |
| | |
| : | : |
| | |

5. Suppose there is some experiment with the following outcomes of -1, 0, 1 or 2.

| k | Pr(X = k) |
|----|-----------|
| -1 | .2 |
| 0 | .3 |
| 1 | .4 |
| 2 | .1 |

| k | $Pr(X^2 = k)$ |
|---|---------------|
| | |
| | |
| | |

| k | $Pr(X^2 + 2 = k)$ |
|---|-------------------|
| | |
| | |
| | |