

2.
$$\min = 1$$
,
 $Q_1 = 2.5$, $Q_2 = 4.5$, $Q_3 = 11.5$, $\max = 23$;
 $IQR = Q_3 - Q_1 = 11.5 - 2.5 = 9$;
 $\begin{vmatrix} 2.5 & 11.5 & 23 \\ 1 & 4.5 & 11.5 & 23 \end{vmatrix}$

3.	Number Waiting in Line	Relative Frequency
	0	0.04
	1	0.10
	2	0.18
	3	0.26
	4	0.22
	5	0.14
	6	0.06

Pr(at most 3 customers in line)

$$= 0.04 + 0.10 + 0.18 + 0.26$$

$$= 0.58$$

4. a. Possible outcomes are HH, HT, TH, TT

Number of Heads,	Pr(X=k)
0	0.25
1	0.50
2	0.25

b.	k	$\Pr(2X + 5 = k)$
	5	0.25
	7	0.50
	9	0.25

5. n = 3, $p = \frac{1}{3}$

1
$$\binom{3}{1} \left(\frac{1}{3}\right)^1 \left(\frac{2}{3}\right)^2 = \frac{12}{27}$$

$$2 \qquad \binom{3}{2} \left(\frac{1}{3}\right)^2 \left(\frac{2}{3}\right)^1 = \frac{6}{27}$$

$$3 \qquad \binom{3}{3} \left(\frac{1}{3}\right)^3 \left(\frac{2}{3}\right)^0 = \frac{1}{27}$$

b.
$$\mu = 0 \left(\frac{8}{27} \right) + 1 \left(\frac{12}{27} \right) + 2 \left(\frac{6}{27} \right) + 3 \left(\frac{1}{27} \right) = 1$$

$$\sigma^2 = (0 - 1)^2 \left(\frac{8}{27} \right) + (1 - 1)^2 \left(\frac{12}{27} \right) + (2 - 1)^2 \left(\frac{6}{27} \right) + (3 - 1)^2 \left(\frac{1}{27} \right)$$

$$= \frac{2}{3}$$

6.
$$n = 4, p = .3$$

$$Pr(X = 2) = {4 \choose 2} (0.3)^2 (0.7)^2 = 0.2646$$

- 7. The student has a .6 probability of guessing correctly on the six questions with answer true and a 0.4 probability of guessing correctly on the four questions with answer false. Therefore the student's expected score is 6(0.6) + 4(0.4) = 5.2 correct answers which gives 52 points or 52%.
 A better strategy is to choose true for all the questions which guarantees a score of 60%.
- 8. a. $Pr(\text{get 7 twice}) = {12 \choose 2} \left(\frac{1}{6}\right)^2 \left(\frac{5}{6}\right)^{10} \approx 0.2961$
 - b. Pr (get 7 at least twice) = 1 - Pr(get 7 zero or one time) = 1 - $\binom{12}{0} \left(\frac{1}{6}\right)^0 \left(\frac{5}{6}\right)^{12} - \binom{12}{1} \left(\frac{1}{6}\right)^1 \left(\frac{5}{6}\right)^{11}$ ≈ 0.6187
 - c. The expected number of 7's is $12 \cdot \frac{1}{6} = 2$.
- 9. $\mu = 0(0.2) + 1(0.3) + 5(0.1) + 10(0.4) = 4.8$ $\sigma^2 = (0 - 4.8)^2(0.2) + (1 - 4.8)^2(0.3) + (5 - 4.8)^2(0.1) + (10 - 4.8)^2(0.4)$ = 19.76
- 10. Let X be the number of red balls.

$$\frac{k}{0} \frac{\Pr(X=k)}{\binom{4}{0}\binom{4}{4}} = \frac{1}{70}$$

$$\frac{\binom{4}{1}\binom{4}{3}}{\binom{8}{4}} = \frac{16}{70}$$

$$\frac{\binom{4}{2}\binom{4}{2}}{\binom{8}{4}} = \frac{36}{70}$$

$$\frac{\binom{4}{3}\binom{4}{1}}{\binom{8}{4}} = \frac{16}{70}$$

$$4 \frac{\binom{4}{4}\binom{4}{0}}{\binom{8}{4}} = \frac{1}{70}$$

$$\mu = 0\left(\frac{1}{70}\right) + 1\left(\frac{16}{70}\right) + 2\left(\frac{36}{70}\right) + 3\left(\frac{16}{70}\right) + 4\left(\frac{1}{70}\right) = 2$$

$$\sigma^2 = (0-2)^2\left(\frac{1}{70}\right) + (1-2)^2\left(\frac{16}{70}\right) + (2-2)^2\left(\frac{36}{70}\right) + (3-2)^2\left(\frac{16}{70}\right) + (4-2)^2\left(\frac{1}{70}\right)$$

$$= \frac{4}{7}$$

11. Xhas mean

$$\mu = (-2)(0.3) + 0(0.1) + 1(0.4) + 3(0.2) = 0.4$$

variance

$$\sigma^2 = (-2 - 0.4)^2 (0.3) + (0 - 0.4)^2 (0.1) + (1 - 0.4)^2 (0.4) + (3 - 0.4)^2 (0.2)$$

= 3.24,

and standard deviation

$$\sigma = \sqrt{3.24} = 1.8$$
.

12. When a pair of fair dice is rolled, the probabilities that the result is 7 or 11 are $\frac{1}{6}$ and $\frac{1}{18}$ respectively. Hence Lucy's expected winnings are $(-10)\frac{2}{9} + 3 \cdot \frac{7}{9} = \frac{1}{9} \approx .11$, or 11 cents per roll.

13.
$$\mu = 10$$
, $\sigma = \frac{1}{3}$
 $10 - c = 9$ and $10 + c = 11$ $c = 1$
Probability: $\ge 1 - \frac{\left(\frac{1}{3}\right)^2}{1^2} = \frac{8}{9}$

14.
$$\mu = 50, \sigma = 8$$

 $50 - c = 38 \text{ and } 50 + c = 62$ $c = 12$
Probability $\ge 1 - \frac{8^2}{12^2} = \frac{5}{9}$

15.
$$\Pr(6.5 \le X \le 11) = \Pr\left(\frac{6.5 - 5}{3} \le Z \le \frac{11 - 5}{3}\right)$$

= $A(2) - A(0.5)$
= $0.9772 - 0.6915$
= 0.2857

16.
$$Pr(Z \ge 0.75) = 1 - 0.7734 = 0.2266$$

17.
$$\mu = 5.75, \sigma = 0.2$$

$$Pr(X \ge 6) = Pr\left(Z \ge \frac{6 - 5.75}{0.2}\right)$$
$$= Pr(Z \ge 1.25)$$
$$= 1 - 0.8944$$
$$= 0.1056$$

10.56%

18.
$$Pr(Z \ge z) = 0.7734$$

 $Pr(Z \le z) = 1 - 0.7734 = 0.2266$

19.
$$\mu = 80, \sigma = 15$$

$$Pr(80 - h \le X \le 80 + h) = 0.8664$$

$$\frac{1 - 0.8664}{2}$$
 = 0.0668 \Rightarrow (area left of 80 - h)

$$Pr(Z \le z) = 0.0668 \text{ when } z = -1.5$$

$$Pr(-1.5 \le Z \le 1.5) = 0.8664$$

Therefore,
$$\frac{x-\mu}{\sigma} = -1.5$$
 and $\frac{x+\mu}{\sigma} = 1.5$.

$$\frac{(80-h)-80}{15} = -1.5 \text{ and } \frac{(80+h)-80}{15} = 1.5$$

$$h = 22.5$$

20. a.
$$Pr(133 \le X) \approx Pr\left(\frac{132.5 - 100}{15} \le Z\right)$$

 $\approx Pr(2.167 \le Z)$
 $\approx Pr(2.20 \le Z)$
 $= 1 - 0.9861$
 $= 0.0139$
 $= 1.39\%$

b.
$$x_{95} = 100 + 15z_{95}$$

= $100 + 15 \cdot 1.65$
= 124.75

21.
$$n = 54$$
, $p = \frac{2}{5}$

$$\mu = 54 \left(\frac{2}{5}\right) = 21.6$$

$$\sigma = \sqrt{54 \left(\frac{2}{5}\right) \left(\frac{3}{5}\right)} = 3.6$$

$$Pr(X \le 13) \approx Pr\left(Z \le \frac{13.5 - 21.6}{3.6}\right) = Pr(Z \le -2.25) = 0.0122$$

22.
$$n = 75$$
, $p = \frac{1}{4}$

$$\mu = 75\left(\frac{1}{4}\right) = 18.75$$

$$\sigma = \sqrt{75\left(\frac{1}{4}\right)\left(\frac{3}{4}\right)} = 3.75$$

$$\Pr(8 \le X \le 22) \approx \Pr\left(\frac{7.5 - 18.75}{3.75} \le Z \le \frac{22.5 - 18.75}{3.75}\right) = \Pr(-3 \le Z \le 1) = 0.8413 - 0.0013 = 0.84$$

Conceptual Exercises

- 23. a. scoring in the third quartile is not very good: 100, 40, 40, 40,
 - b. scoring in the third quartile corresponds to a perfect grade: 100, 100, 90, 80, 70
- 24. a. The mean and median are equal: 1, 2, 3, 4, 5, 6, 7, 8, 9, 10: The mean is 5.5; the median is 5.5
 - b. the mean is less than the median: 1, 1, 1, 1, 4, 5, 6, 7, 8, 9: The mean is 4.3; the median is 4.5
 - c. the median is less than the mean 1, 2, 3, 4, 5, 6, 10, 12, 14, 100. The median is 5.5; the mean is 15.7
- 25. A population mean is the average of all the data in the entire population. When a sample is taken from a population, the sample mean is the average of all the data in that particular sample. Sample means vary whereas the population mean is fixed.
- 26. A sample mean is taken from the population and is the average of all the data values in a particular sample, which is a subset of the population.
- Yes; in general, if we add a constant to each number in a set, then the mean will increase by that constant.
- 28. Yes; in general, if we multiply each number in a set by some constant, then the standard deviation will be multiplied by that constant.
- 29. The binomial probability distribution applies when there is a fixed number of independent trials when the probability of success is constant. The outcome of each trial is classified as either a "success" or a "failure".
- Repeated trials that do not produce a binomial distribution: 1) tossing a coin until a head appears. 2) Having children until a girl is born.