Name:

Problem	1 / 2	3	4 / 5	6 / 7	Total
Possible	32	21	16	31	100
Received					

DO NOT OPEN YOUR EXAM UNTIL TOLD TO DO SO.

You may use a 3 x 5 card of notes, both sides, and a calculator.

FOR FULL CREDIT, SHOW ALL WORK RELATED TO FINDING EACH SOLUTION.

FIND THE FINAL ACTUAL VALUE FOR ALL PROBLEMS.



MUTTS By Patrick McDonnell



- 17 points 1. Suppose that a person is a 55% free throw shooter. She will shoot 10 shots.
 - /5 What is the probability of making exactly 7 shots?
 - /10 What is the probability of making <u>at least</u> 2 of the 10 shots?
 - /2 What is the *expected number* of shots she would make? That is, if she were to shoot 10 shots, and then another 10 shots, and then another 10 shots, over and over, then on average how many shots (out of 10) would she make?

- 15 points 2. Consider the investment at right.
 - /5 Find the expected value of the investment:

Return	Probability
-4	.5
2	.1
7	.4

/10 Find the variance and standard deviation of the investment:

z $A(z)$ z	A(z)
-3 50 0002 -2 00	0228
-345 0003 -195	0256
-3.40 .0003 -1.90	.0287
-3.35 .0004 -1.85	.0322
-3.30 .0005 -1.80	.0359
-3.25 .0006 -1.75	.0401
-3.20 .0007 -1.70	.0446
-3.15 .0008 -1.65	.0495
-3.10 .0010 -1.60	.0548
-3.05 .0011 -1.55	.0606
-3.00 .0013 -1.50	.0668
-2.95 .0016 -1.45	.0735
-2.90 .0019 -1.40	.0808
-2.85 .0022 -1.35	.0885
-2.80 .0026 -1.30	.0968
-2.75 .0030 -1.25	.1056
-2.70 .0035 -1.20	.1151
-2.65 .0040 -1.15	.1251
-2.60 .0047 -1.10	.1357
-2.55 .0054 -1.05	.1469
-2.50 .0062 -1.00	.1587
-2.45 .0071 95	.1711
-2.40 .0082 90	.1841
-2.35 .0094 85	.1977
-2.30 .0107 80	.2119
-2.25 .0122 75	.2266
-2.20 .0139 70	.2420
-2.15 .0158 65	.2578
-2.10 .0179 60	.2743
-2.05 .0202 55	.2912
-	
$z A(z) \mid z$	
	A(z)
- 50 3085 1.00	A(z)

z	A(z)	z	A(z)
	0005	1.00	0.410
50	.3085	1.00	.8413
45	.3264	1.05	.8531
40	.3446	1.10	.8643
35	.3632	1.15	.8749
30	.3821	1.20	.8849
25	.4013	1.25	.8944
20	.4207	1.30	.9032
15	.4404	1.35	.9115
10	.4602	1.40	.9192
05	.4801	1.45	.9265
.00	.5000	1.50	.9332
.05	.5199	1.55	.9394
.10	.5398	1.60	.9452
.15	.5596	1.65	.9505
.20	.5793	1.70	.9554
.25	.5987	1.75	.9599
.30	.6179	1.80	.9641
.35	.6368	1.85	.9678
.40	.6554	1.90	.9713
.45	.6736	1.95	.9744
.50	.6915	2.00	.9772
.55	.7088	2.05	.9798
.60	.7257	2.10	.9821
.65	.7422	2.15	.9842
.70	.7580	2.20	.9861
.75	.7734	2.25	.9878
.80	.7881	2.30	.9893
.85	.8023	2.35	.9906
.90	.8159	2.40	.9918
.95	.8289	2.45	.9929

21 points	3. The heights of a certain population of corn plants follow a		
	normal distribution with mean 140 cm and standard		
	deviation 10 cm.		

/5 What percentage of the plant heights are 130 cm or less?

- /2 What percentage of the plant heights are 130 cm or more?
- /1 What percentage of the plant heights are **exactly** 130 cm?
- /8 What percentage of the plant heights are between 130 and 145 cm?

/5 What is the plant height at the 40th percentile?

10 points
4. Suppose you flip 3 coins. We are interested in the number of heads, which we call X.
/8 Find the probability distribution for the number of heads:



- /2 What is the expected number of heads?
- 5. Suppose there are 80 people to be tested for Covid. If each person has his/her own individual test, then 80 tests will be administered and analyzed. Suppose instead that all 80 are tested ("pooled") together. If that one test is negative, then we're done: all 80 people are Covid-free. But if the pooled test is positive, then one (or more) person in the group has Covid, thus all 80 will then be tested individually. Find the expected number of tests to be administered in this "pooled testing" approach. You can start by completing the table below. Assume that 0.5% (so 0.005) of the population being tested actually have Covid. Simplify/evaluate your answer below for expect number of tests.

Outcome of pooled test	Total number of tests given	Probability
Positive	81	
Negative	1	

Expected number of tests per 80 people =

11 points 6. Find (and **show appropriate work**) the mean, variance and standard deviation of the following ten values:

 $2 \quad 2 \quad 2 \quad 2 \quad 2 \quad 2 \quad 5 \quad 5 \quad 10 \quad 10 \quad 10$

20 points 7. Suppose we roll a die 10 times. We are interested in getting fives. /5 What is the probability of getting exactly 2 fives?

Use the normal curve to approximate the next two probabilities.

/9 What is the probability of getting at least 2 fives?

/6 What is the probability of getting exactly 2 fives? (Remember to use the **normal curve** to approximate this value.)