Calculation of Isotopic Abundances

Problem 2-44

What are the percent natural abundances of the two naturally occurring isotopes of boron, ¹⁰B and ¹¹B? These isotopes have masses of 10.012937 u and 11.009305 u, respectively.

Solution

Weighted-average atomic mass = WAAM WAAM = $abund_1 \times AM_1 + abund_2 \times AM_2$ $abund_1 + abund_2 = 1$ $abund_2 = 1 - abund_1$ The WAAM for boron is 10.811 u (from the periodic table)

$$\begin{split} 10.811 & \texttt{u} = abund_1 \times 10.012937 \ \texttt{u} + abund_2 \times 11.009305 \ \texttt{u} \\ & = abund_1 \times 10.012937 \ \texttt{u} + (1 - abund_1) \times 11.009305 \ \texttt{u} \\ & = abund_1 \times 10.012937 \ \texttt{u} + 11.009305 \ \texttt{u} - abund_1 \times 11.009305 \ \texttt{u} \\ & -0.198305 \ \texttt{u} = abund_1 \times 10.012937 \ \texttt{u} - abund_1 \times 11.009305 \ \texttt{u} \\ & = -0.996368 \times abund_1 \\ abund_1 = 0.19903 \qquad (= 19.903\%^{-10}\text{B}) \\ abund_2 = 1 - 0.19903 = 0.80097 \qquad (= 80.097\%^{-11}\text{B}) \end{split}$$